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OPEN DATA CHALLENGE

Deep Generative Models for Creating Synthetic Microstructures

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Objective

- A key problem in computational material science deals with understanding the effect of material distribution (i.e., microstructure) on material performance.
- The challenge we consider here is to **synthesize microstructures with desired physical and chemical properties**, given a finite number of microstructure images, evaluated based on the **physical invariances that the microstructure exhibits**.
- Conventional approaches are based on stochastic optimization and are computationally intensive.
- We introduce Machine learning based generative models for the **fast synthesis of binary microstructure** images.
- Our model is a Wasserstein Generative Adversarial Network that uses a finite number of training images to synthesize new microstructures that satisfy the physical invariances respected by the original data.
- For the training of our model, we curated a dataset of **Binary 2D microstructural images of polymer phase separation**. We made our dataset available publically.
 - In this presentation, we discuss:
 - 1. Details of **dataset generation**
 - 2. Physical invariances under consideration: volume fraction and two-point correlation
 - 3. Introduction to deep generative adversarial networks (GANs) and our method.
 - 4. Microstructure images generated by our WGAN model, and their analysis
 - 5. Conclusion on usefulness and effectiveness of our model

1.1 Dataset

We curated a dataset of Binary 2D microstructural images of polymer phase separation (CH - dataset).

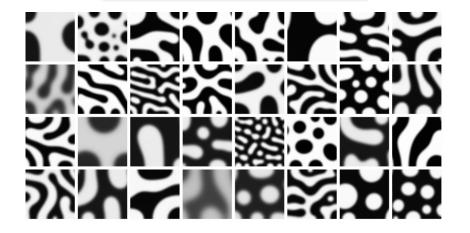
- This dataset was generated through the simulation of a time evolving Cahn -Hilliard equation [1], describing phase separation in binary polymer blends. Thus, we call it CH-dataset.
- Several realizations of the equation were done through different values of volume fractions and binary interaction parameters.
- Morphologies were outputted at constant time intervals.

Details of the dataset

- Collection of 34672 grayscale images,
- resolution of each image is 101x101.
- Each pixel takes a floating point value between 0 and 1.
- Dataset and supporting code is made public at:

https://zenodo.org/record/2580293

Samples from the dataset



1.2 Dataset Generation

dataset was generated through the simulation of a time evolving Cahn -Hilliard equation [1]:

$$\frac{\partial \phi}{\partial t} = \nabla \left(M \nabla \left(\frac{\partial f}{\partial \phi} - \epsilon^2 \nabla^2 \phi \right) \right)$$
$$f(\phi) = \phi \ln(\phi) + (1 - \phi) \ln(1 - \phi) + \chi_{12} \phi (1 - \phi)$$

- Simulations were performed on a 101×101 (pixels) square domain, for 10 values of $\chi_{12} \in [2.2, 3.4]$; 10 values of total volume fraction $\phi_0 = \int_{\Omega} \phi d\Omega \in [0.3, 0.5]$. Also, $\epsilon = 1e - 2$, l_x , $l_y = 1$, M = 1, dt = 1e - 3.
- Data was saved after every prescribed number of time steps (20 time steps).
- Data was then augmented by reflecting and flipping the phases(black/white)
- Because data was generated using an **energy dissipating equation**, data generated using one simulation has:
 - The same (volume) fraction for all times ($\int_{\Omega} \phi d\Omega = constant \ \forall \ t$),
 - With increasing time, the average domain size increases as $r_{avg} \propto t^{\frac{1}{3}}$. i.e., r_{avg} increases with time.

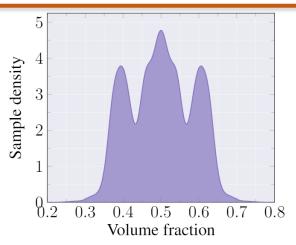
2. Physical Invariances

We consider the underlying material to be a **two-phase homogeneous**, **isotropic** material. Our setup for statistical characterization of microstructure follows with [2].

- A phase function $\phi^{(1)}(.)$ is used to characterize this two-phase system, defined as: $\phi^{(1)}(r) = \begin{cases} 1, r \in V_1, \\ 0, r \in V_2, \end{cases}$ where V_1 is the region occupied by phase 1 and V_2 is the region occupied by phase 2.
- The 1-point correlation function, $p_1^{(1)}$, commonly known as **volume fraction**, is defined as: $p_1^{(1)} = \mathbb{E}_r \phi^{(1)}(r)$
- The two-point correlation function, $p_2^{(1)}$, is defined as: $p_2^{(1)}(r_{12}) = \mathbb{E}_{r_1,r_2}[\phi^{(1)}(r_1) \phi^{(1)}(r_2)]$

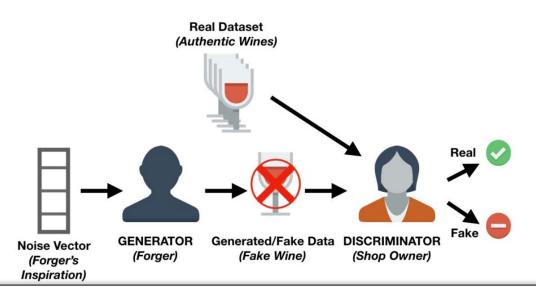
- Our aim is to synthesize microstructures that satisfy certain target statistical properties of the material distribution.
- We choose these statistical properties to be total volume fraction of a material (p₁) and 2-point correlation (p₂).

Distribution of volume fraction for our dataset



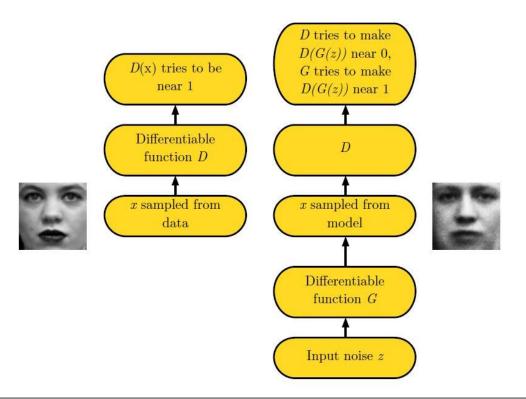
3.1 Introduction to Generative Adversarial Networks [4]

The basic idea of GANs is to set up a minimax game between two players: generator and discriminator [4].



- We can think of the generator as being like a forger, trying to make fake wine, and the discriminator as being like wine-shop owner, trying to allow legitimate wines and catch fake wines.
- To succeed in this game, the forger must learn to make wine that is
 indistinguishable from genuine wine implying that the generator network must
 learn to create samples that are drawn from the same distribution as the
 training data.

GAN model

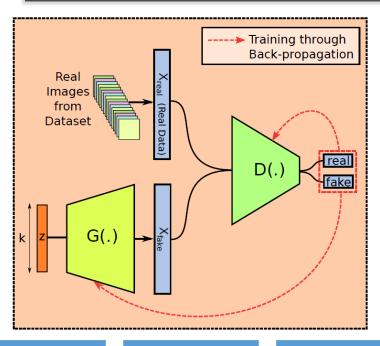


$$\min_{G} \max_{D} V(D, G) = E_{x \sim p_{data}(x)}[log D(x)] + E_{z \sim p_{z}(z)}[log(1 - D(G(z)))]$$

Image credits: (left) datacamp blog, (right) GAN tutorial by Ian Goodfellow

3.2 Our methodology

We use our CH dataset as the training data for a improved version of GAN – called Wasserstein GAN with Gradient Penalty [5].



WGAN-GP-CH

 Trained over CH dataset that contains all 34672 images covering entire range of p1 and p2.

WGAN-GP-CHp1

to 0.45.

 Trained over CHp1 dataset with ~6000 images of CH images of CH dataset having a volume fraction (p₁) value between 0.35 0.0625.

WGAN-GP-CHp2

 Trained over CHp2 dataset with~3000 dataset having a (p₂) value equal to

- Using the Cahn-Hilliard (CH) dataset, we prepare two smaller datasets referred as CHp1 and CHp2 by segregating the images based on their p_1 and p_2 values respectively.
- The first subset **CHp1** is a collection of all images of CH dataset having a volume fraction (p₁) value between 0.35 to 0.45.
- The second subset is segregated on the basis of p_2 values of images, and contain all the images from CH dataset having 2 – point correlation (p_2) value equal to 0.0625.
- We train 3 WGAN-GP using CH, CHp1 and CHp2 as the training data respectively.
- As these segregated datasets typically contain images with similar statistical properties (either p_1 or p_2), we can testify the ability of our model to preserve such properties by observing the p1 or p2 values of the images generated by these 3 networks.

4.1 Results

Our trained WGAN-GP models are able to generate microstructures closely resembling the real microstructures. Moreover, these generated microstructures respect the statistical constraints (p_1 and p_2)

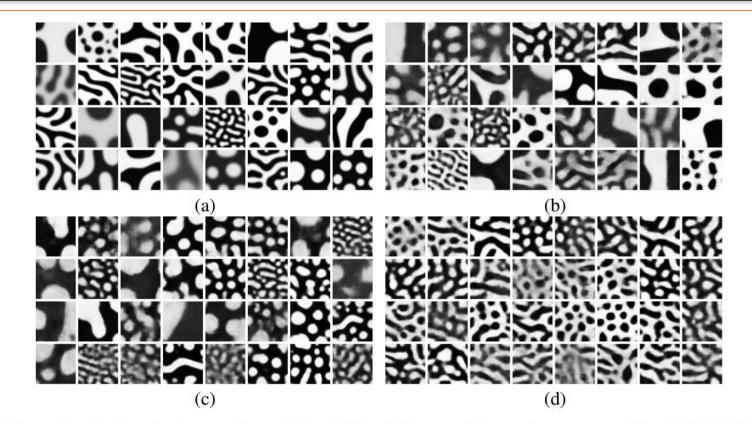


Figure 2: (a) Sample images from Cahn-Hilliard dataset; (b) samples generated by WGAN-GP trained on CH-dataset; (c) Samples generated by WGAN-GP trained over the morphologies from CH_{p1} dataset (only includes the images with volume fraction between 0.35 to 0.45); (d) Samples generated by WGAN-GP trained over the morphologies from CH_{p2} dataset (only includes the images with 2-point correlation equal to 0.0625).

4.2 Analysis of the Results

We analyze (i) the **statistical properties** of the generated miscrostructures; (ii) **interpolation behavior** of our trained WGAN models; (iii) **Free energy of generated microstructures** to present interesting findings.

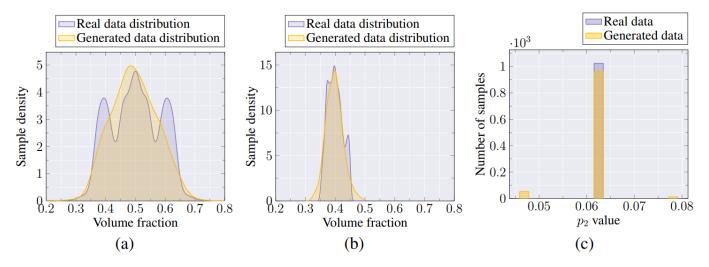


Figure 3: (a) Comparisons of the distributions of volume fractions of training dataset and that of the samples generated by WGAN-GP trained over entire CH dataset; (b) Comparisons of the distributions of volume fractions of training dataset and that of the samples generated by WGAN-GP trained over the CH_{p1} dataset; (c) Histograms of p_2 correlation values for samples from CH_{p2} dataset and samples generated by WGAN-GP trained over CH_{p2} dataset.

- Fig. 3 provides the density plots/histograms of p_1 and p_2 values of the images for both training data and generated data.
- The striking similarities in the spread of both the density plots/histograms suggest that our **network successfully reproduces the statistical properties** of the real (training) images in the simulated images.
- In Fig. 3 (a,b), densities of p₁ value is compared between the real data and generated data for network trained on CH dataset and CHp1 dataset.
- We provide the histogram for p2 values for models trained using CHp2 in Fig. 3 (c). Both the histograms closely match.

4.3 Analysis of the Results

We display interesting behavior of the learned image manifold through results of interpolation over latent vectors z

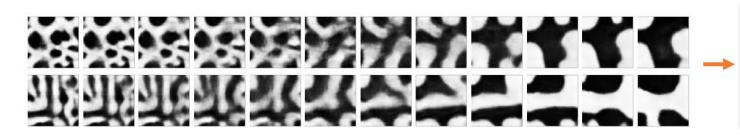


Figure 4: (a) Results of the linear interpolation over latent variable z for WGAN-GP trained over the entire CH dataset

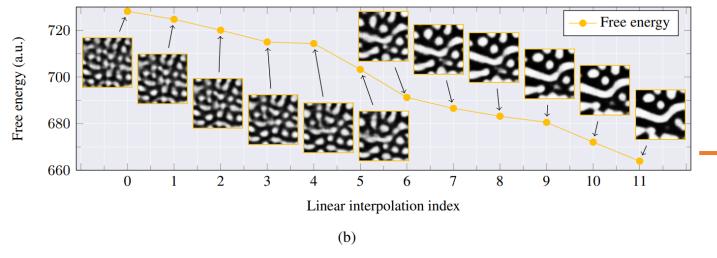


Figure 5: (a) Results of the linear interpolation over latent variable z for WGAN-GP trained over the images from CH_{p1} dataset (only includes the images with volume fraction between 0.35 to 0.45); volume fraction values are printed above each image; (b) Free energy of the interpolated morphologies (volume fraction of each image is $(0.41 \pm 5\%)$.

Randomly pick two different noise vectors z₁ and z₂, and linearly interpolate between them to obtain 10 more such noise vectors. All 12 images are plotted as in Fig. 4.

- Very interestingly, we observe that an unseen invariance of energy minimization is captured in the interpolation. As shown in Fig. 5 (b), the free energy of the morphologies decreases as the we move from one interpolation step to the next.
- In this process, the volume fraction (p₁) is also preserved within reasonable limits. This suggests that the WGAN framework is able to learn latent physical rules from the dataset.
- Such behavior can effectively be used to decide series of manufacturing processes for obtaining final morphology from initial morphology without adding any new material.

5. Conclusion

- We curated a **Binary 2D microstructural images of polymer phase separation (CH dataset)** by solving CH equations and successfully used it with a machine learning model that **approaches computational results in microstructure synthesis tasks**.
- We also made our dataset publically available.
- We train three different WGAN models with full or subset of our CH dataset. We show that the generated images **respect** the distribution of certain physical invariances specifically, can be used for synthesizing a promising new material that meets a desired performance target.
- We analyze our results to come up with interesting properties of our trained WGAN models such as interpolation and free energy reduction behavior and explore previously unknown correlations in process-structure-property linkages.

References

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